

Show all work on a ***separate sheet*** of paper. **This review is not comprehensive, be sure to study your old notes, tests, and homework assignments!**

1. Divide the following and express the answer in the form: $q(x) + \frac{r}{\text{divisor}}$:

a) $(6x^2 - 7x - 5) \div (3x - 5)$

c) $(7x^2 - 23x + 6) \div (x - 3)$

b) $(3x^2 + 5x^3 + 1) \div (x + 2)$

d) $(x^4 - 5x + 10) \div (x + 3)$

2. Show that $(x - 2)$ is a factor of $P(x) = x^3 - 3x^2 - 10x + 24$, and find the other two factors.

3. What is the remainder when $3x^{107} + 14x^{35} - 16x$ is divided by $(x - 1)$?

4. What is the remainder when $14x^{10} - 2x^3 - 17$ is divided by $(x + 2)$?

5. Determine if $(x + 3)$ is a factor of $f(x) = x^3 + x^2 - 5x + 3$

6. Determine if $(x + 1)$ is a factor of $f(x) = x^3 - 13x^2 + 23x - 11$

7. If $(x + 16)$ is a factor of $f(x)$ then what is one of the zeros?

8. If $(2x - 3)$ is a factor of $f(x)$ then what is one of the roots?

9. If $f(x) = (x - 3)(2x - 1)(3 + x)$ then what are the roots?

10. If $f(8) = 0$, what is one of the factors of $f(x)$?

11. If $f\left(\frac{3}{2}\right) = 0$, what is one of the factors of $f(x)$?

For questions 12-15 find the complete factorization:

12. $f(x) = x^3 + 2x^2 - 8x$

13. $P(x) = x^3 - 5x^2 - 4x + 20$

14. $P(x) = x^3 - 2x^2 + 4x - 8$

15. $P(x) = 2x^5 - 28x^3 - 64x$

For questions 16-18 find the solution set of $f(x)=0$:

16. $f(x) = 3x^3 + 11x^2 + 5x - 3$; (hint: -1 is a zero)

17. $f(x) = (x^2 + 3x + 5)(2x + 3)$

18. $f(x) = 2x^5 - 28x^3 - 64x$

19. Determine the equation of a cubic function whose zeros are -1, -2, and -3

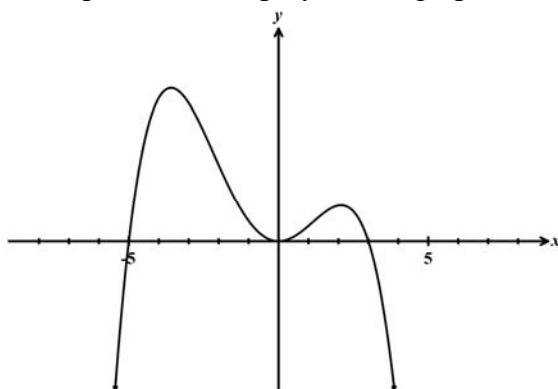
20. Which of the following could be the equation of the polynomial graph shown below?

(1) $y = -x(x+5)(x-3)$

(2) $y = x(x+3)(x-5)$

(3) $y = -x^2(x+5)(x-3)$

(4) $y = x^2(x+3)(x-5)$



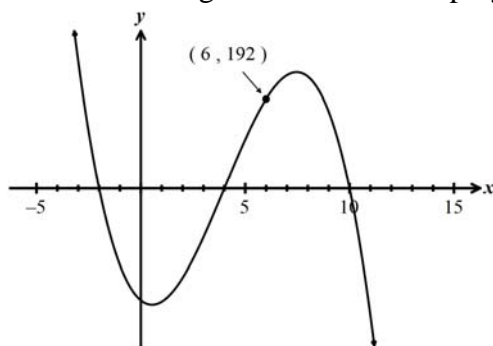
21. The cubic polynomial shown graphed below passes through the point $(6, 192)$ as shown. Which of the following is the value of the leading coefficient of the polynomial?

(1) -7

(2) -3

(3) $\frac{1}{3}$

(4) 5



22. Which of the following is a factor of the cubic polynomial $x^3 - 10x^2 + 11x + 70$?

(1) $x+10$

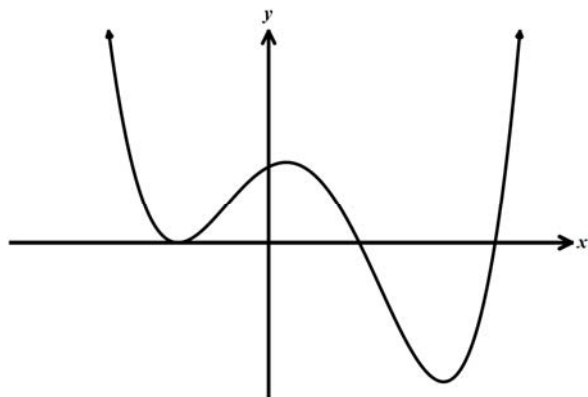
(3) $x-7$

(2) $x-2$

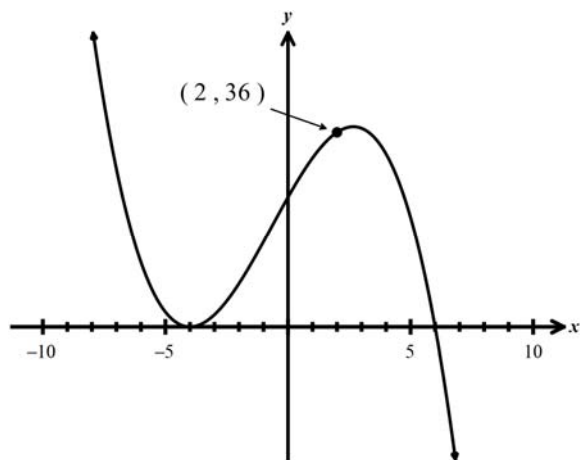
(4) $x+5$

23. Given the cubic polynomial $f(x) = x^3 - 5x^2 - 4x + 20$ answer the following.

- Find the x -intercepts of this function algebraically. Show how you arrived at your answer.
- Explain why the graph below could *not* represent that of $f(x)$.



24. The cubic polynomial below has zeroes at $x = -4$ and $x = 6$ only and passes through the point $(2, 36)$ as shown. Algebraically determine its equation in factored form. Show how you arrived at your answer.



25. The rational expression $\frac{4x^3 - 2x^2 + 8x + 10}{x - 5}$ can be written as $p(x) + \frac{k}{x - 5}$, where $p(x)$ is a quadratic polynomial and k is a constant.

- Determine the equation for $p(x)$. Show how you arrived at your answer.
- Is $x - 5$ a factor of $4x^3 - 2x^2 + 8x + 10$? Explain how your reasoning.

